

DESIGN OF TENSION MEMBERS



INTRODUCTION

Characteristics

- **Members Experience**
 - **Axial force**
 - **Stretching**
 - **Uniform stress over the cross section**
- **Very Efficient Member**
 - **Strength governed by the material strength**
 - **Bolt holes affect the strength**

INTRODUCTION

Applications:

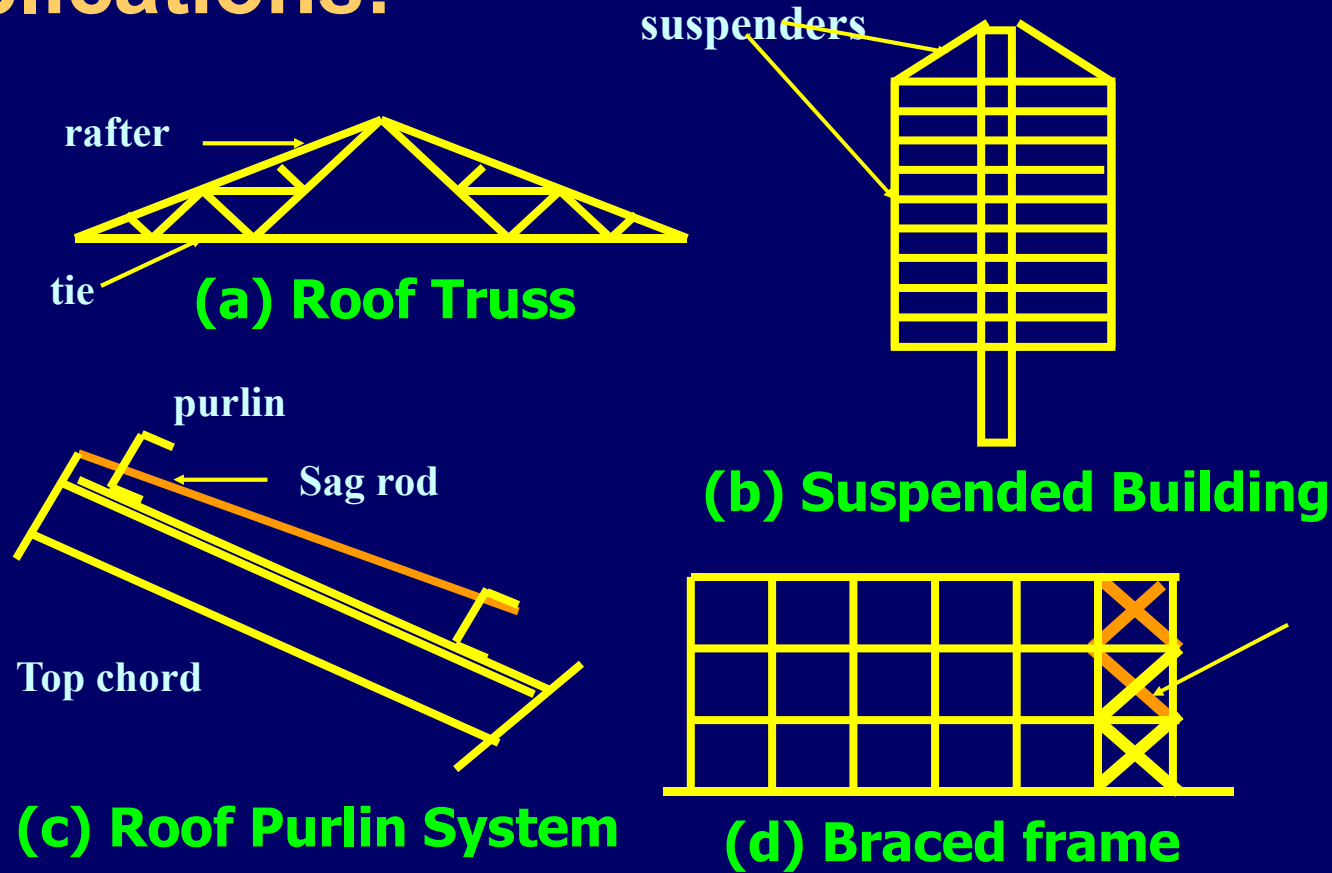


Fig.1(a) Tension Members in Buildings

INTRODUCTION

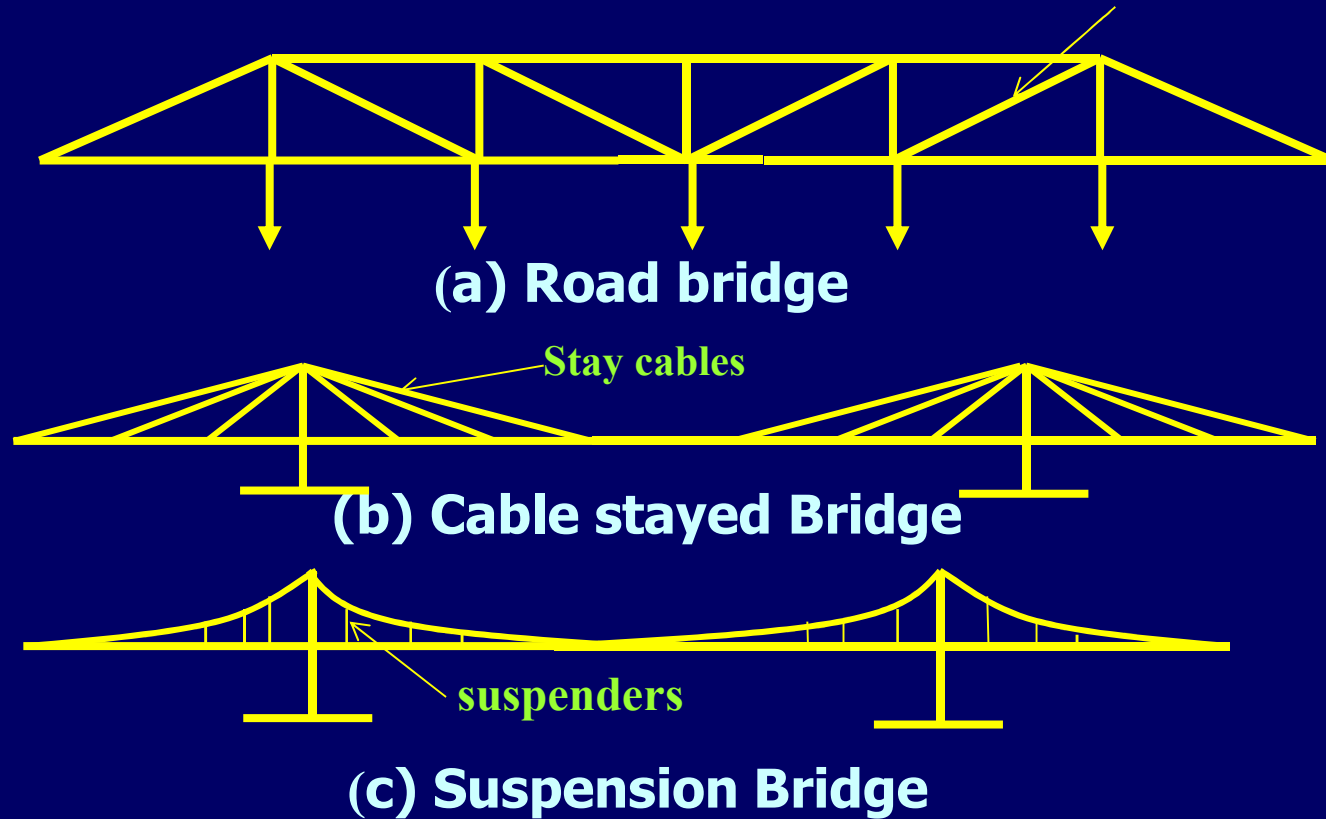
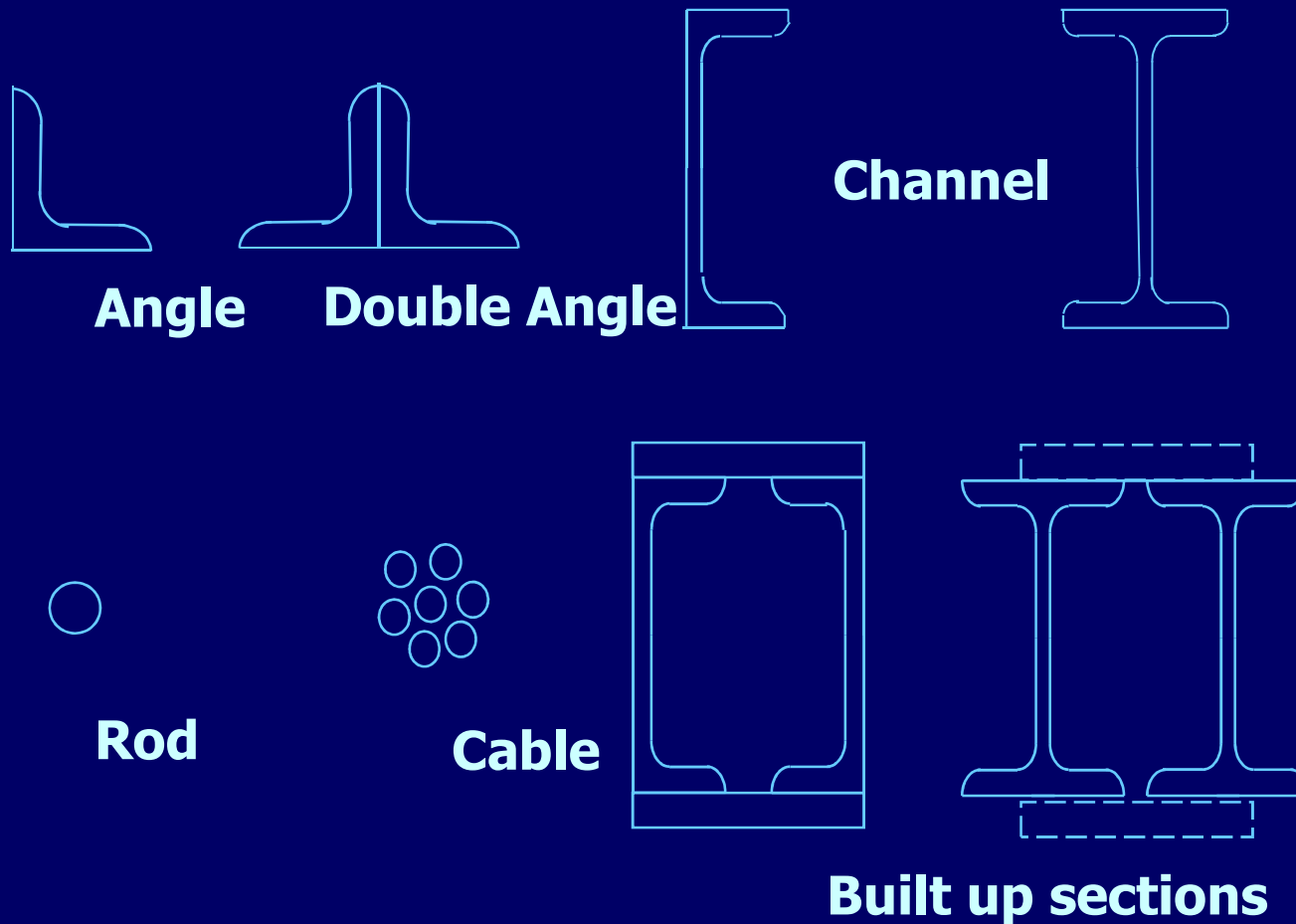


Fig.1(b) Tension Members in Bridges

INTRODUCTION

Cross Sections Used for Tension Members



INTRODUCTION



INTRODUCTION

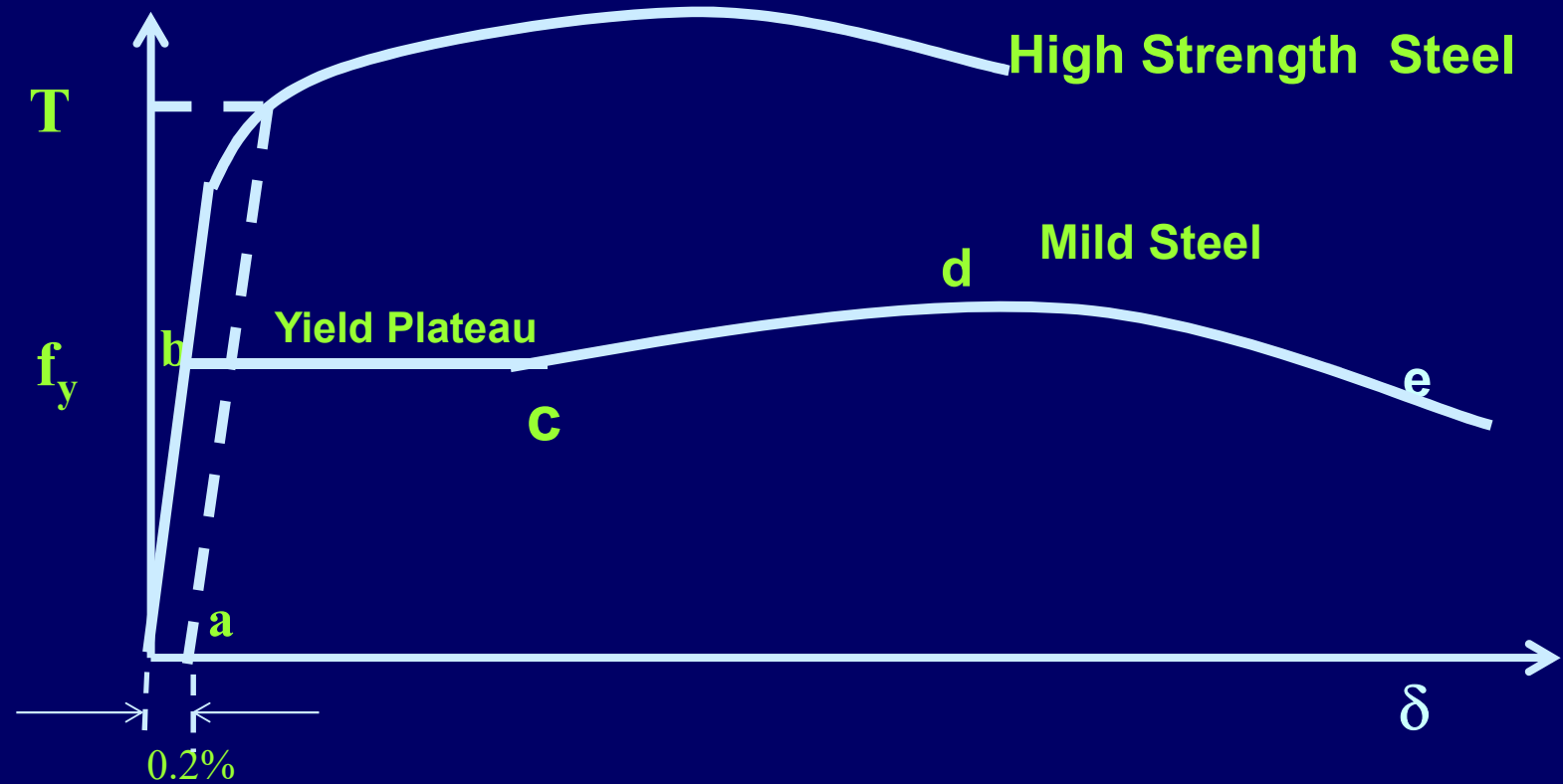


INTRODUCTION



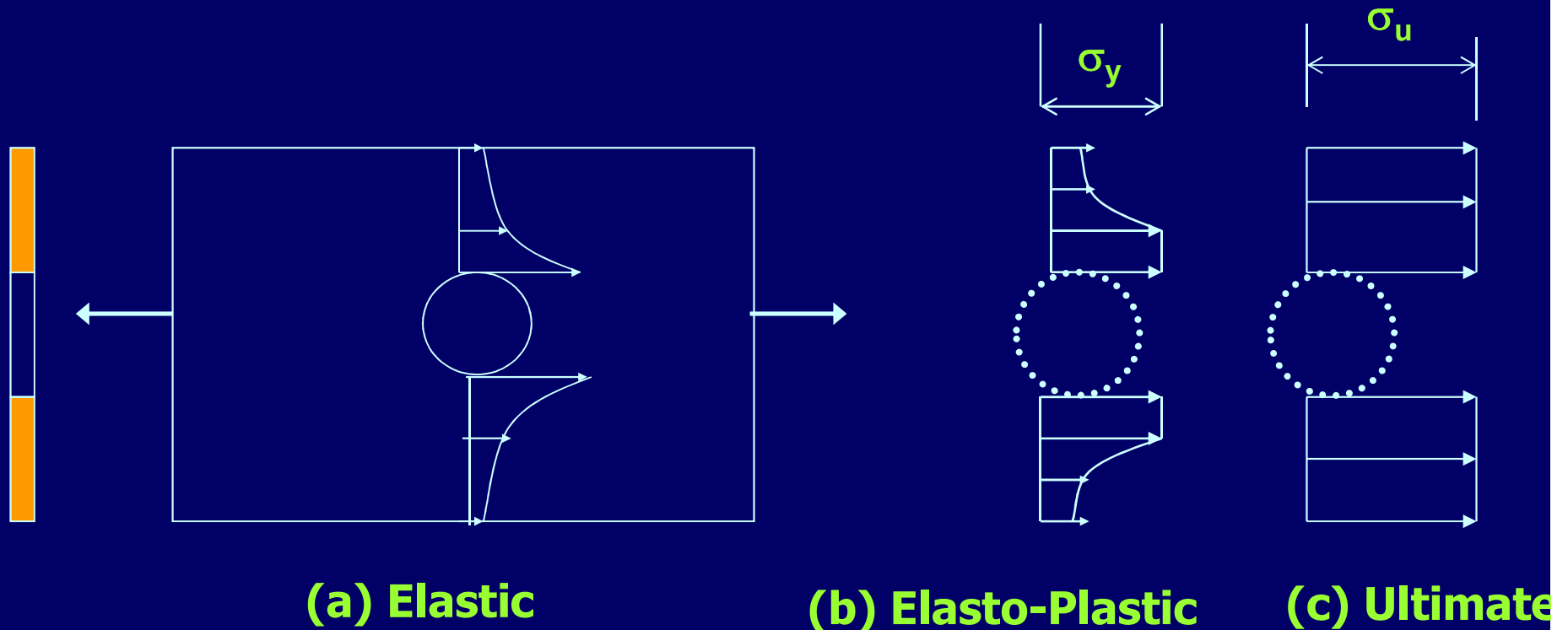
BEHAVIOUR IN TENSION

Material Properties



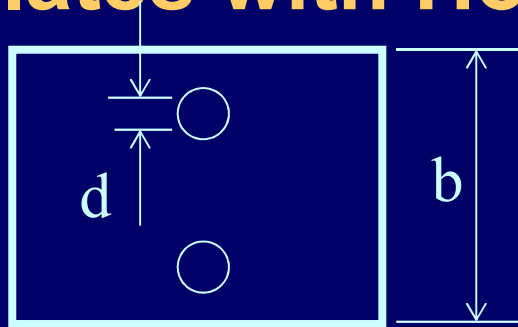
BEHAVIOUR IN TENSION

Plates with a Hole



BEHAVIOUR IN TENSION

Plates with Holes



(a)



(b)

Case a:

$$\text{Net Area: } = t (b - 2*d)$$

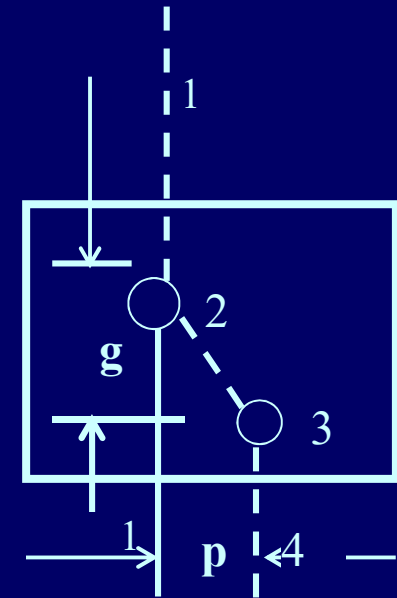
Case b:

$$\text{Net Area: } = t (b - d)$$

Case c:

$$\text{Net Area: } < t (b - d)$$

$$> t (b - 2*d)$$

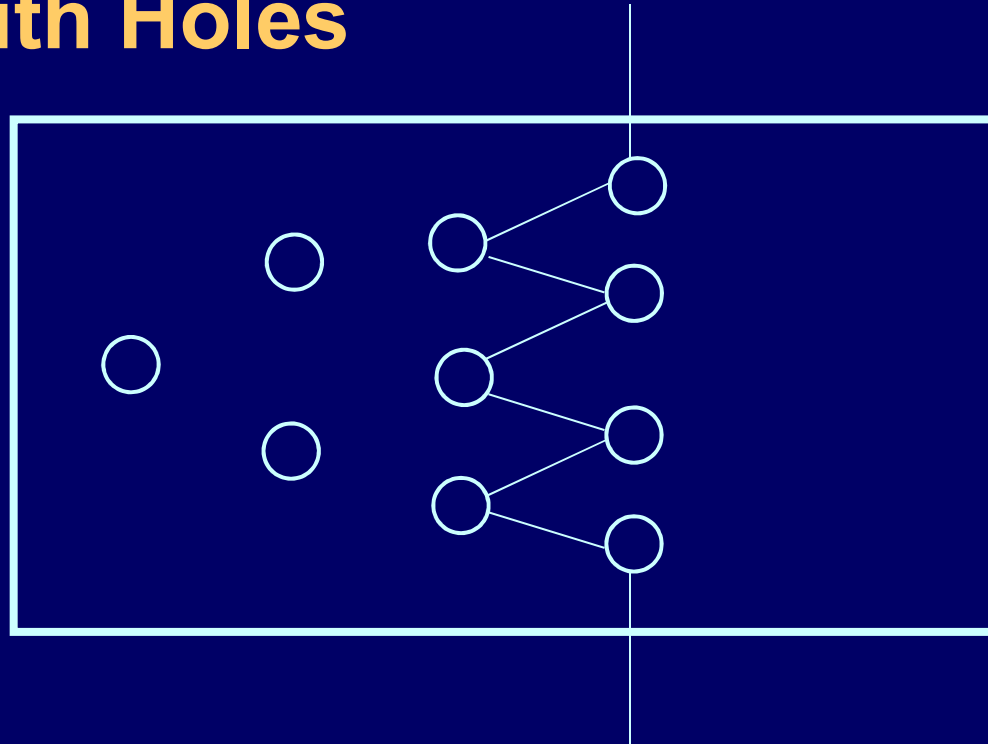


P = pitch

g = gauge

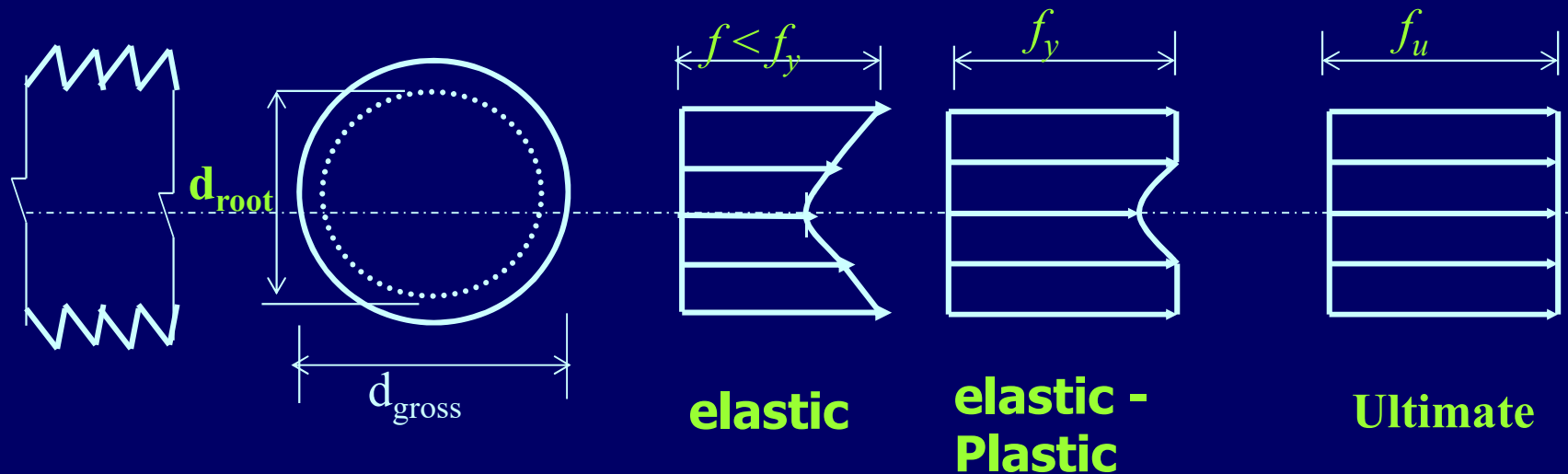
BEHAVIOUR IN TENSION

Plates with Holes



$$A_n = [b - n d + \Sigma(p^2 / 4 g)]$$

BEHAVIOUR IN TENSION



Gross Area Design Strength (P_{tg})

$$P_{tg} = f_y * A_g / \gamma_{MO}$$

$$\gamma_{MO} = 1.15$$

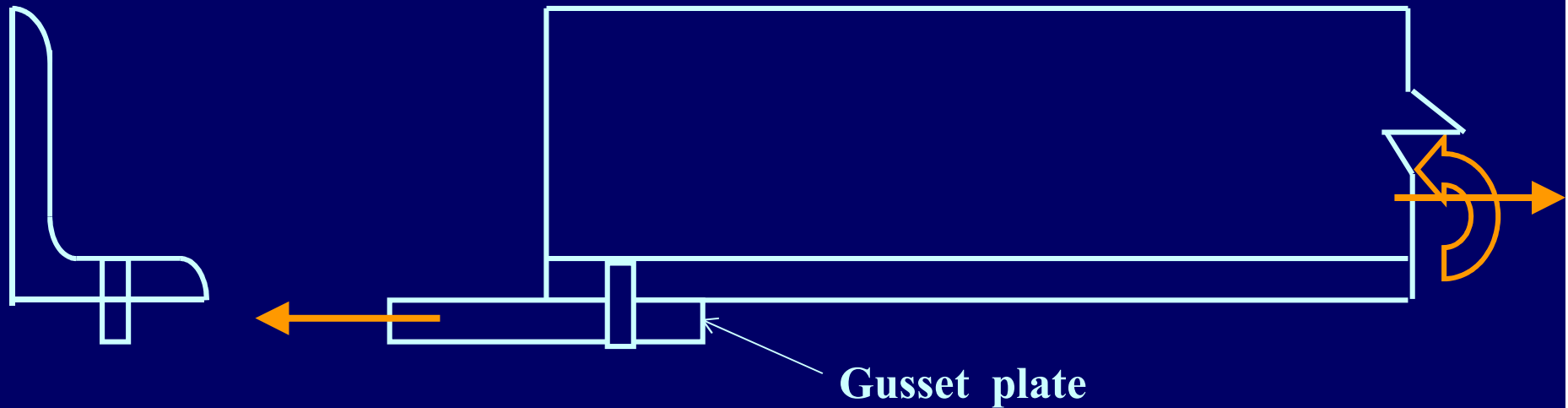
Net Area Design Strength (P_{tn})

$$P_{tn} = 0.9 * f_u * A_n / \gamma_{M1}$$

$$\gamma_{M1} = 1.25$$

BEHAVIOUR IN TENSION

- **ANGLES** Eccentrically Loaded Through Gussets



ANGLES UNDER TENSION

- **Factors Affecting Angle Strength**
 - **Effect of Gusset Thickness**
 - **Effect of Angle Thickness**
 - **Effect of Shear Lag**
 - **Effect of End Connections**
 - **Effect of Block Shear**

- **Shear Lag**
 - Plate when subjected to tension are subjected to shear deformation near edges . (Tensile stress near to zero at edges)
 - Shear stress produced in material gradually transfer tension at edges to central axis of plate.
 - Transfer of stresses take place in the length of member approximately equal to its width
 - Beyond this length tensile stresses are assumed to be uniformly distributed over the whole section of plate.
 - Transmission of tension at edges to full width by shear stress is Shear lag
- In case of I- beam, internal transfer of force from flange to web is by shear
- In case of angles transfer of forces from on leg to other is by shear

ANGLES UNDER TENSION

Effect of Shear Lag

Shear Lag → Strength Reduction

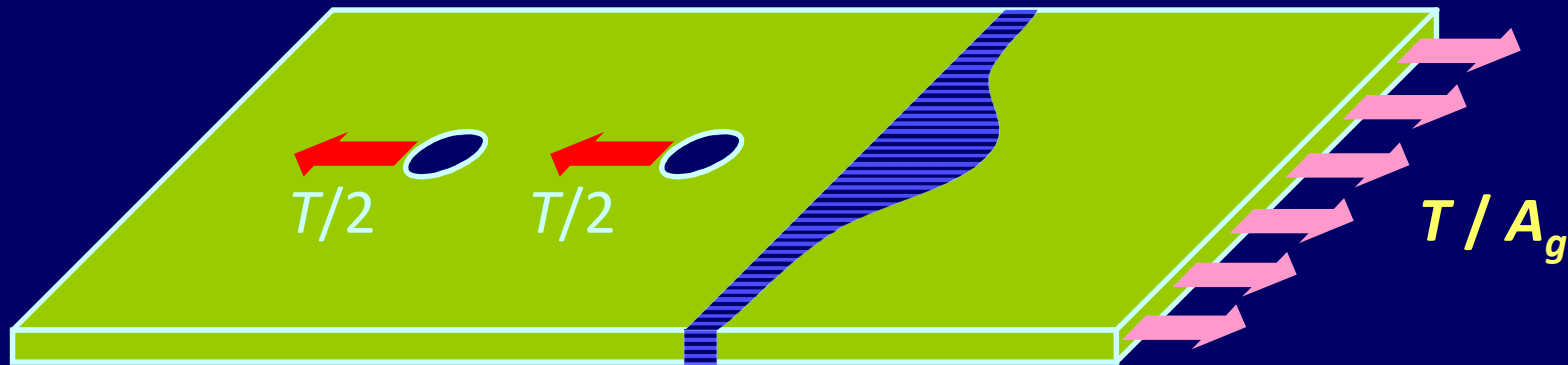
Shear Lag ↑ as A_o / A_g ↑

Shear Lag ↓ as end connection Stiffness ↑

Non-Uniform Stress

More stress near restraint

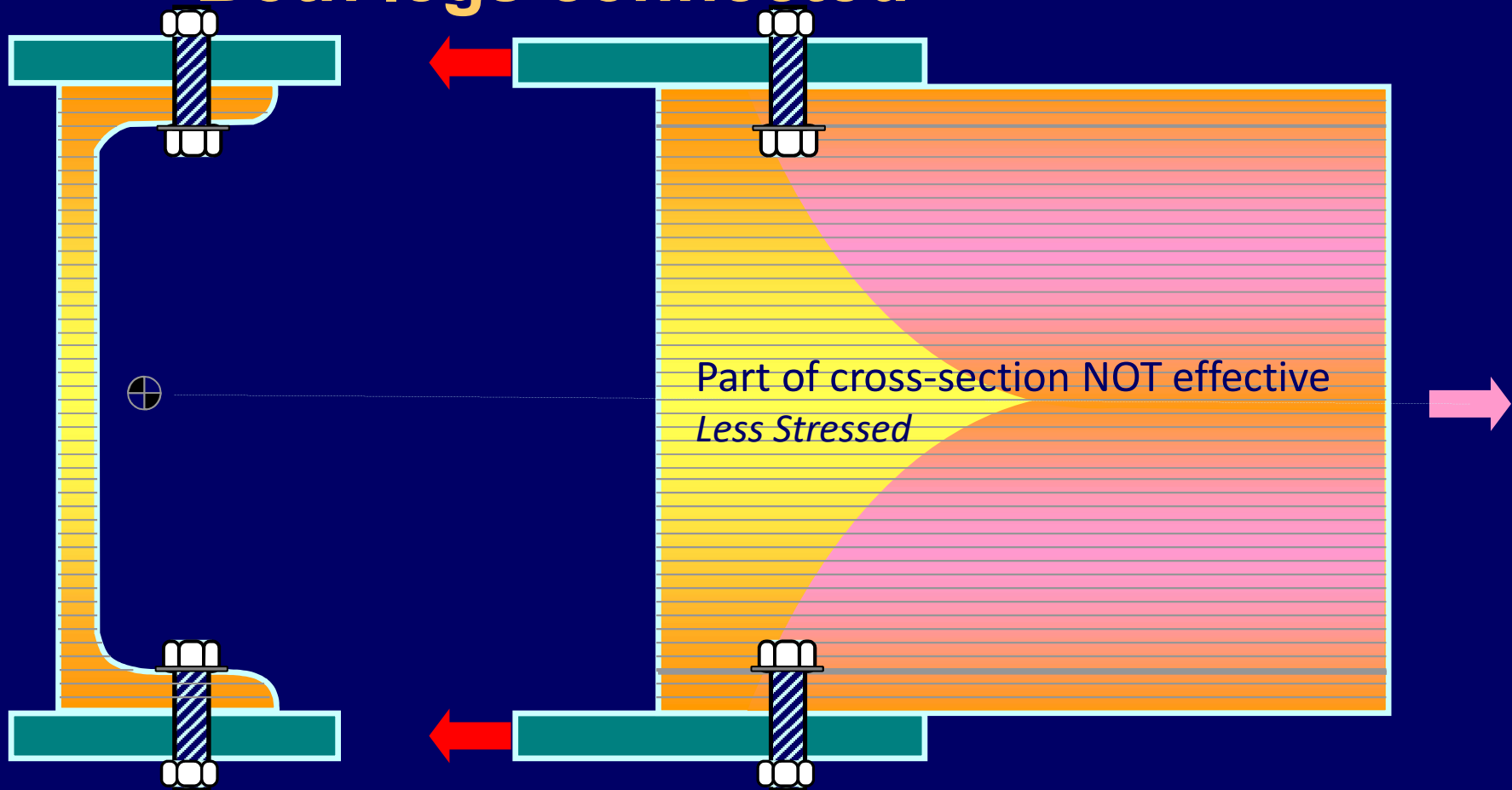
Less stress near un-restrained / free ends



Shear Lag

Channels

Both legs connected



Shear Lag...

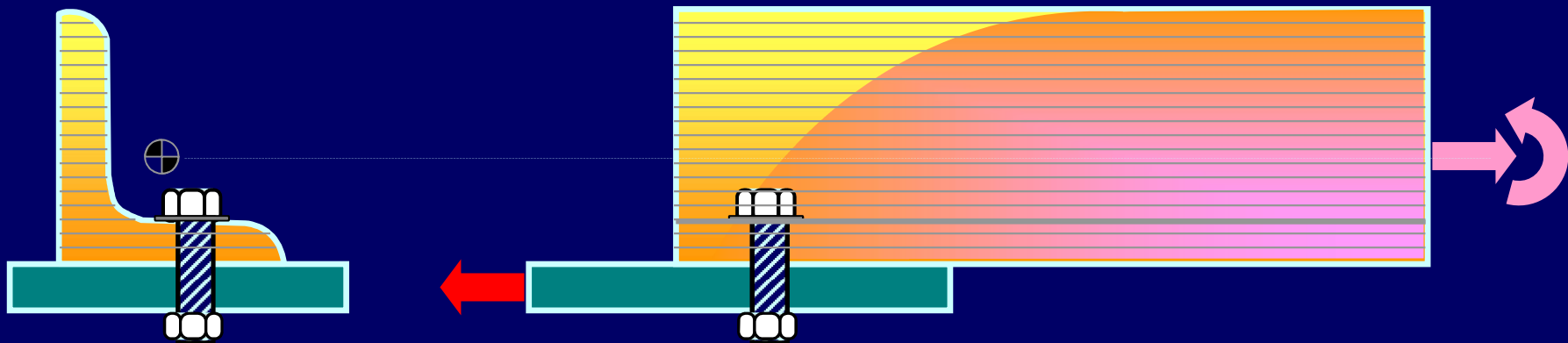
Angles

Single leg connected

Eccentrically loaded through gusset plates

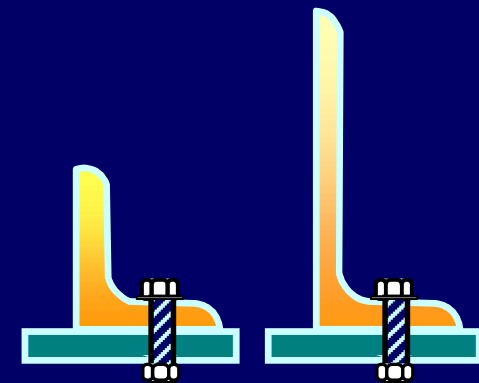
Free,
Un-stiffened,
Un-connected end

Part of cross-section NOT effective Less Stressed



Shear Lag...

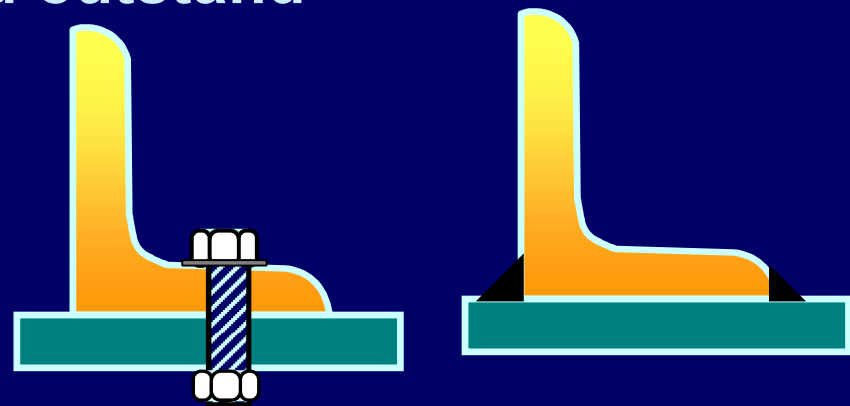
- **Effects of Shear Lag**
 - **Strength reduction**
 - Part of cross-section ineffective (less stressed)
 - Consider in *Design*
- **Factors affecting / causing Shear Lag**
 - **Outstand (unconnected part)**
 - More outstand – more shear lag
 - Thin / slender outstand – more shear lag
 - **Connection stiffness**
 - Flexible connection – more shear lag



- **Rupture of net section**

$$T_{dn} = 0.9 \times A_{nc} \times f_u / \gamma_{m1} + \beta \times A_{go} \times f_y / \gamma_{m0}$$

- A_{nc} = Net area of the *connected* leg
- A_{go} = Gross area of the *unconnected* leg
- β = reduction factor based on contribution of unconnected outstand



Angles in Tension...

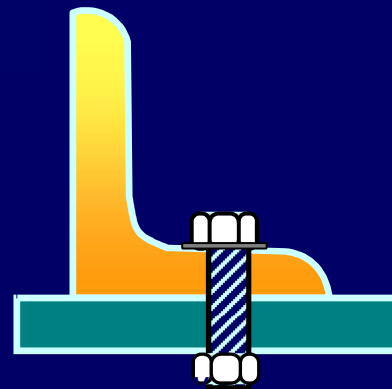
- Rupture of net section**

$$T_{dn} = 0.9 \times A_{nc} \times f_u / \gamma_{m1} + \beta \times A_{go} \times f_y / \gamma_{m0}$$

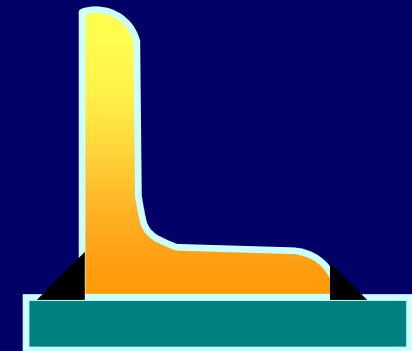
$$\beta = 1.4 - 0.076 \left(\frac{w}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_s}{L_c} \right)$$

$$\leq \left(\frac{f_u}{f_y} \right) \left(\frac{\gamma_{m0}}{\gamma_{m1}} \right)$$

$$\geq 0.7$$



$$b_s = w + w_1 - t$$



$$b_s = w$$

Angles in Tension...

Rupture of net section

Limits of $(\beta \times A_{go} \times f_y / \gamma_{m0})$

- **Upper limit:** $A_{go} \times f_u / \gamma_{m1}$
 - Full unconnected length rupture
- **Lower limit:** $0.7 \times A_{go} \times f_y / \gamma_{m0}$
 - 70% of unconnected length yielding

$$\begin{aligned}\beta &= 1.4 - 0.076 \left(\frac{w}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_s}{L_c} \right) \\ &\leq \left(\frac{f_u}{f_y} \right) \left(\frac{\gamma_{m0}}{\gamma_{m1}} \right) \\ &\geq 0.7\end{aligned}$$

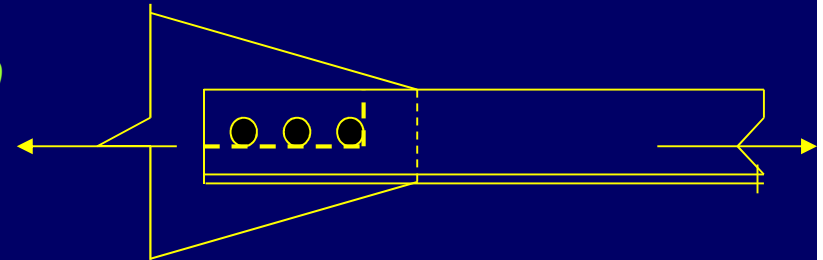
ANGLES UNDER TENSION

Strength of Net Section

$$P_{tn} = A_{nc} * f_u / \gamma_{M1} + \beta * A_o f_y / \gamma_{M0}$$

Strength of Gross Section

$$P_{tg} = A_g * f_y / \gamma_{M0}$$



Block Shear Strength

$$\begin{aligned} P_{tb} &= (0.62 * A_{vg} * f_y / \gamma_{M0} + A_{tn} * f_u / \gamma_{M1}) \\ &= (0.62 * A_{vn} * f_u / \gamma_{M1} + A_{tg} * f_n / \gamma_{M0}) \end{aligned}$$

DESIGN OF TENSION MEMBERS

Efficiency

$$\eta = P_t / (A_g * f_y / \gamma_{M0})$$

Design Steps

$$A_n = P_t / (f_u / \gamma_{M1})$$

$$A_g = P_t / (f_y / \gamma_{M0})$$

Choose a trial section

Analyse for its strength

DESIGN OF TENSION MEMBERS

Stiffness Requirements

Designed for compression under
stress reversal

$$l/r < 250$$

*Not designed for compression under
stress reversal*

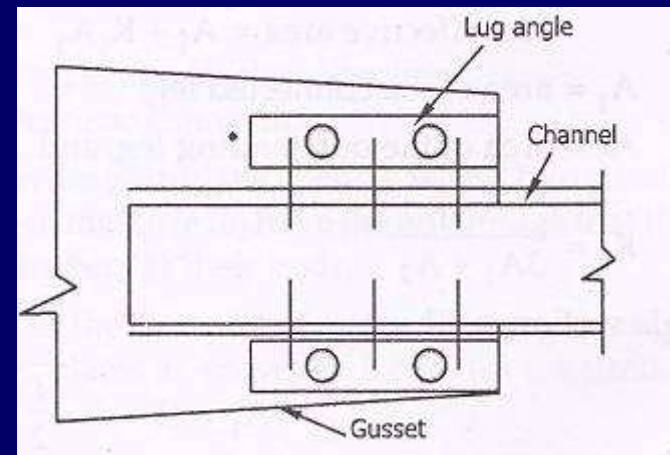
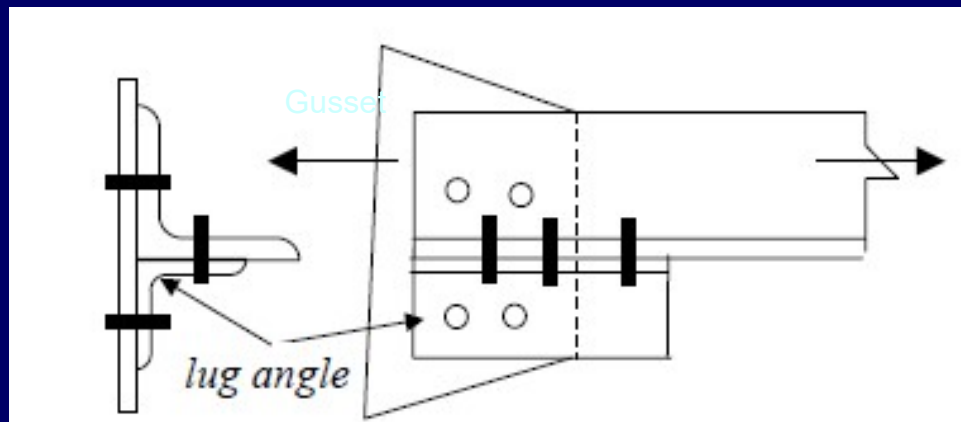
$$l/r < 350$$

Members under tension only

$$l/r < 400$$

LUG ANGLE

- A short length of angle section
- Attached to the main tension member at the connecting end

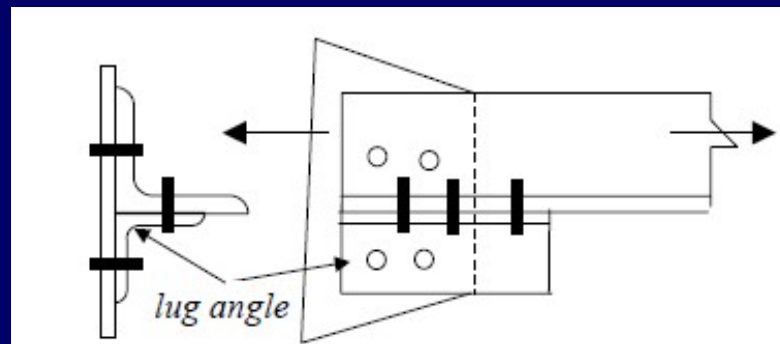


ADVANTAGES

- **When a tension member is connected to a gusset plate at its end, a large number of bolts are required, specially when the tensile load is large, necessitating the provision of big size gusset plate**
- **Size of the gusset plate decreased**
- **Providing extra gauge lines for accommodating the required number of bolts.**
- **Increase the efficiency of the outstanding leg and to decrease the length of the end connections**

How IS 800-2007 view Lug Angle?

- **Effective connection of the lug angle**
 - terminate at the end of the member
 - connection start in advance of the member of the gusset plate
 - minimum of two bolts, rivets or equivalent welds



If the main member is an angle

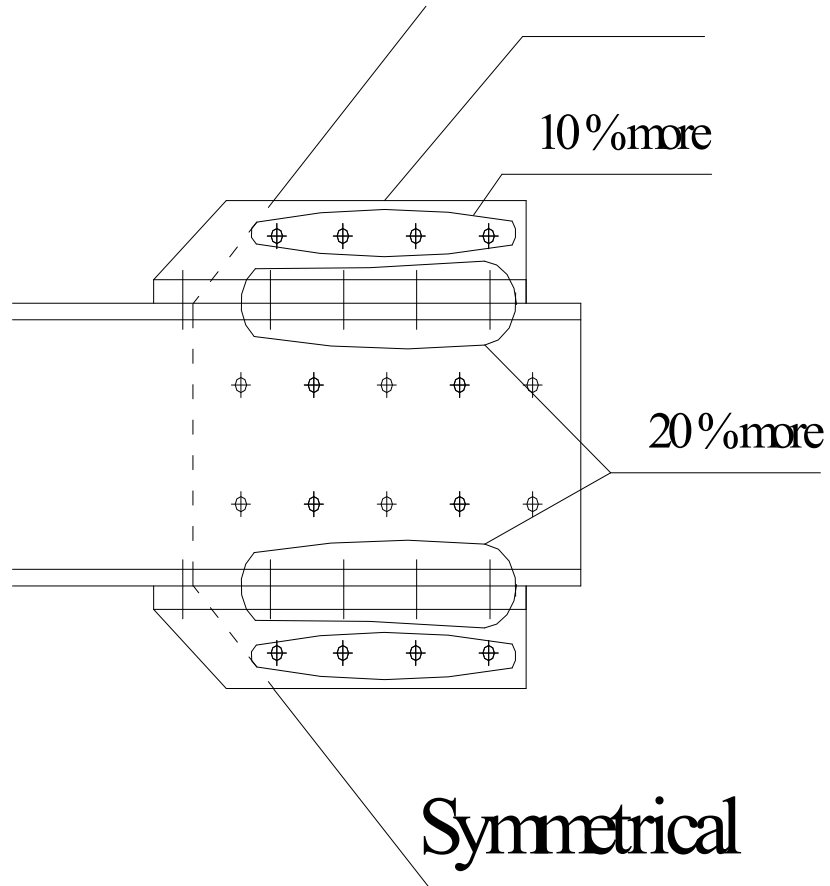
- **whole area of the member shall be taken as the effective (whole area = gross area – deduction for bolt holes)**
- **lug angle to gusset plate = 20% more than the force in outstanding leg**
- **lug angle to main member = 40% more than the force in outstanding leg**

Lug angle....

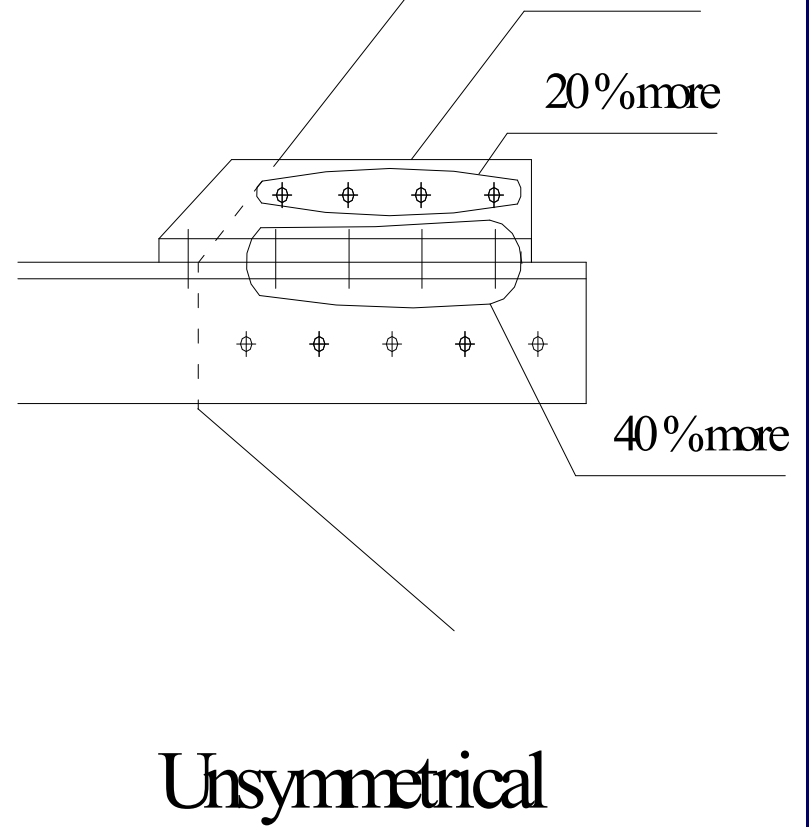
If the main member is a channel

- **Symmetric**
- **lug angle to gusset plate = 10% more than the force in outstanding leg**
- **lug angle to main member = 20% more than the force in outstanding leg**

Lug angle

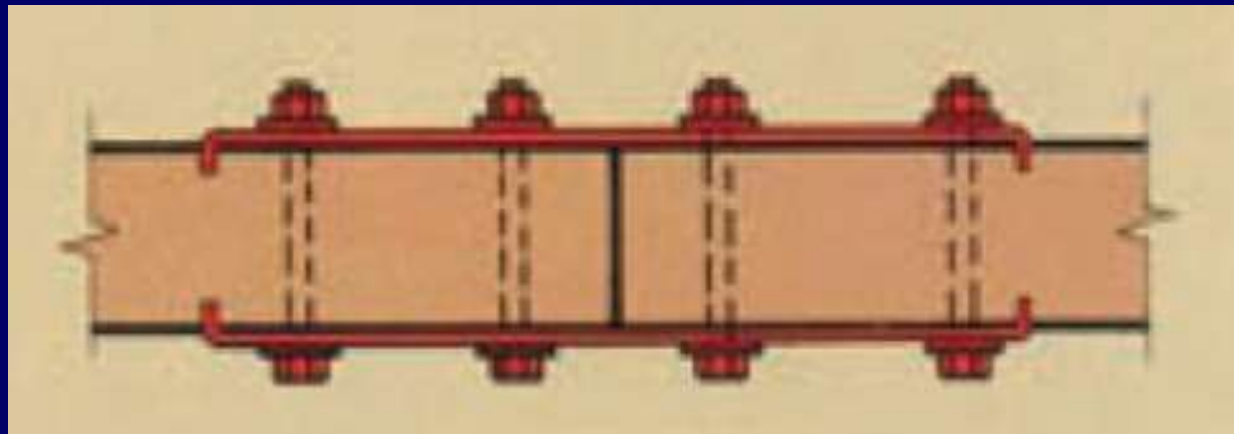


Lug angle

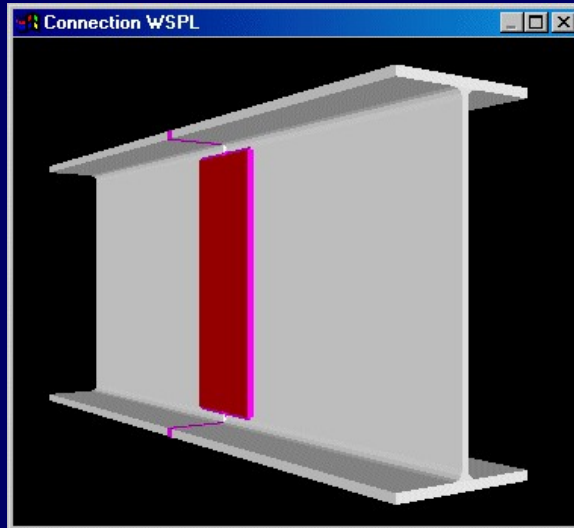


Tension splice

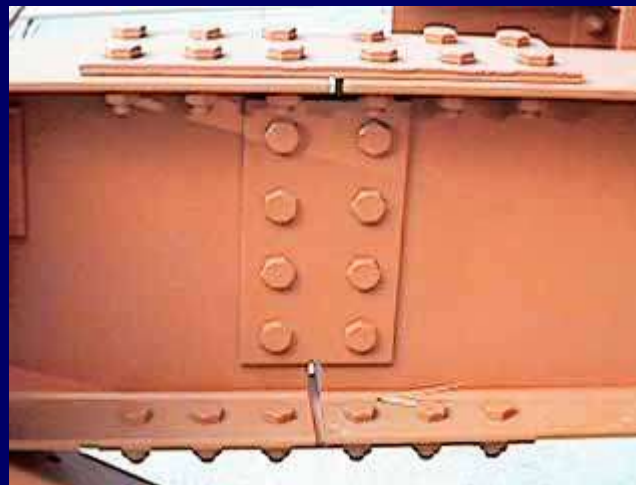
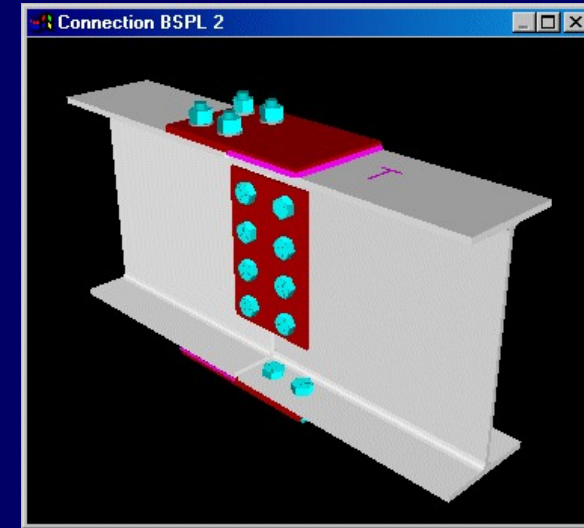
- **Tension members spliced.....**
 - Tension member is less than available length
 - different thicknesses



- **Web splice**

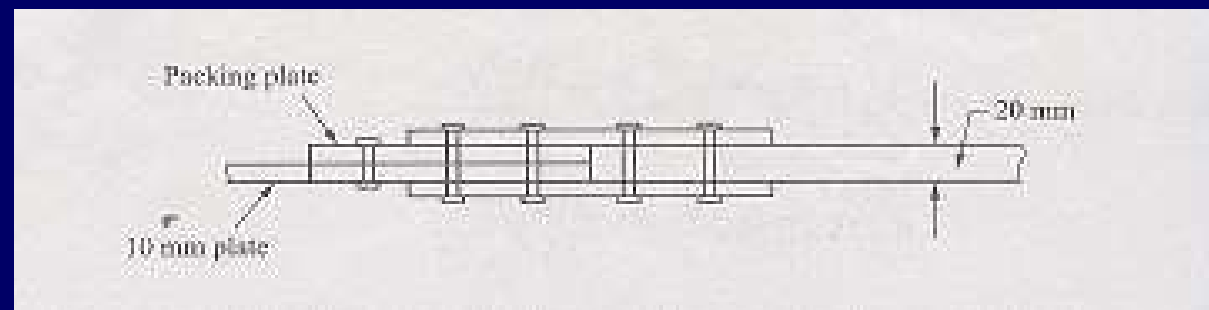


Flange splice



Tension splice....

- both the sides of the member - cover plates – to form a butt joint
- bolts placed to transfer the load
- Plates of different thickness
 - Filler plates or packing plates



Tension splice....

How IS 800-2007 view Tension splice ?

- **Strength of the splice plate and bolts – design load**
- **Design shear capacity of bolts carrying shear through packing plates in excess of 6mm**

$$\beta_{pk} = 1 - 0.0125t_{pk}$$

Tension splice

Filler plates

- **Additional bolts – thickness of packing plate >6 mm**
- **For each 2mm thickness of packing, number increased by 2.5 %.**